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(54) **VOLUMETRIC IMAGING OF HOLOGRAPHIC OPTICAL TRAPS**

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(51) **Int. Cl.**  
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**H01S 1/00** (2006.01)  
**H01S 3/00** (2006.01)  
**H05H 3/02** (2006.01)

(52) **U.S. Cl.** ..... **359/15; 250/251**

(58) **Field of Classification Search** ..... **359/1, 15; 250/251**

See application file for complete search history.

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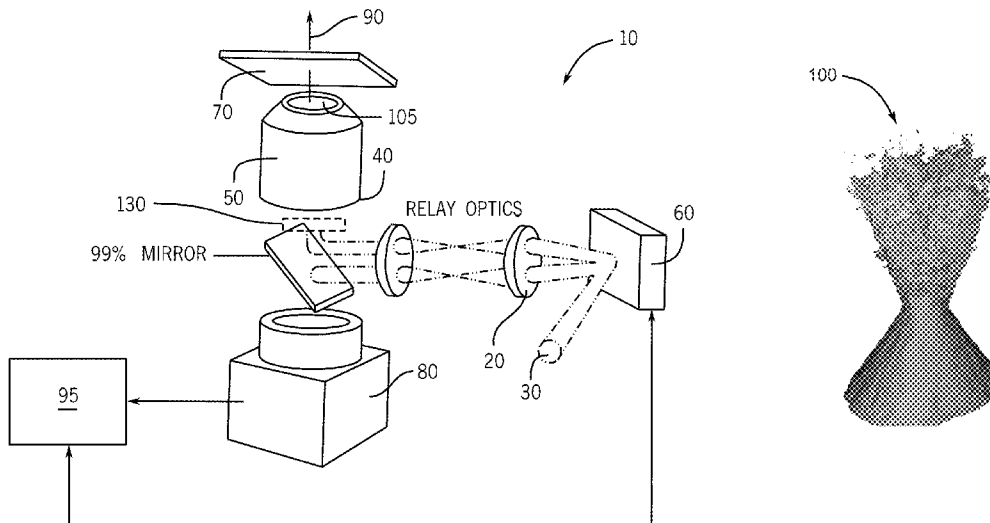
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(57) **ABSTRACT**

A method and system for manipulating object using a three dimensional optical trap configuration. By use of selected hologram on optical strap can be configured as a preselected three dimensional configuration for a variety of complex uses. The system can include various optical train components, such as partially transmissive mirrors and Keplerian telescope components to provide advantageously three dimensional optical traps.

**21 Claims, 6 Drawing Sheets**



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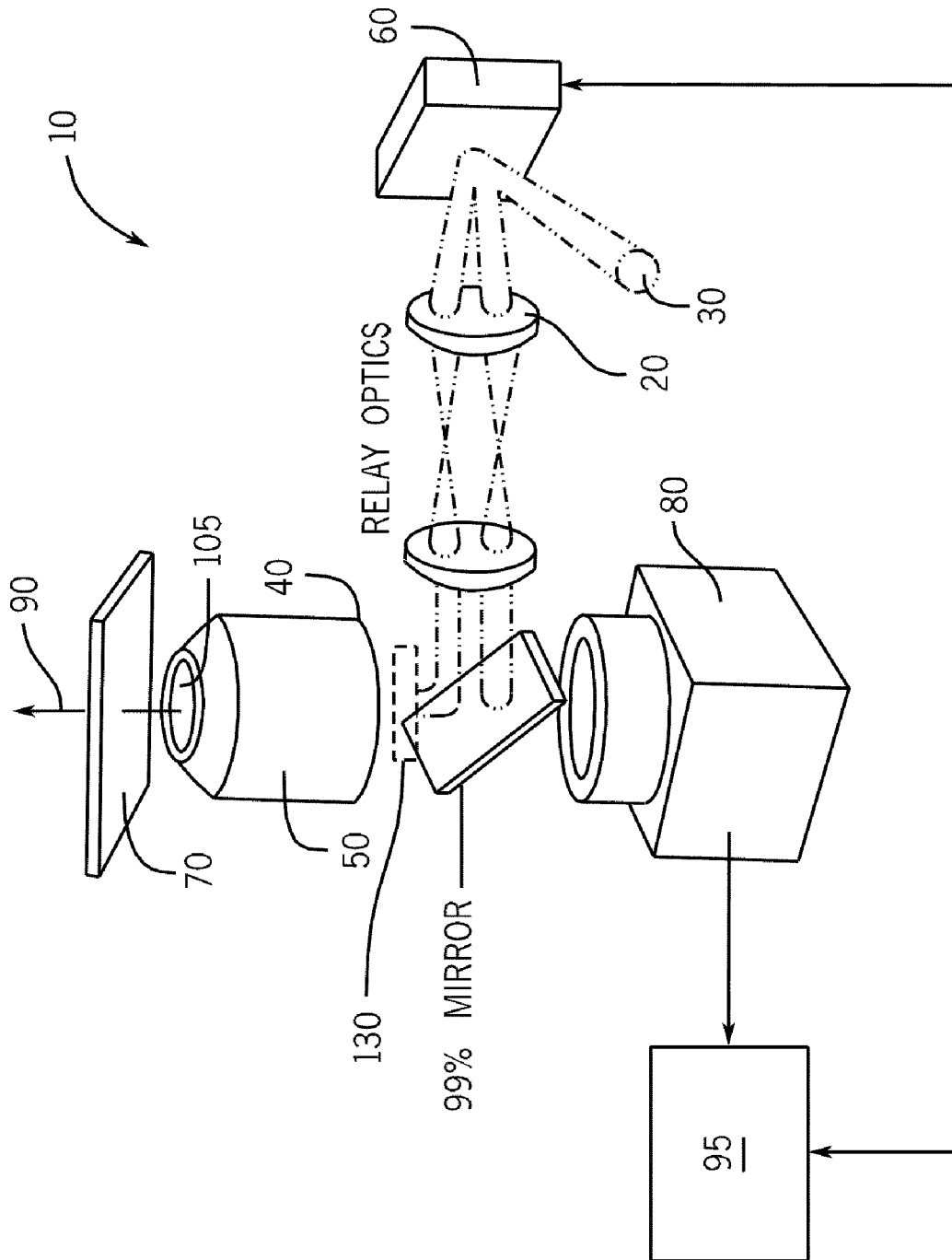


FIG. 1

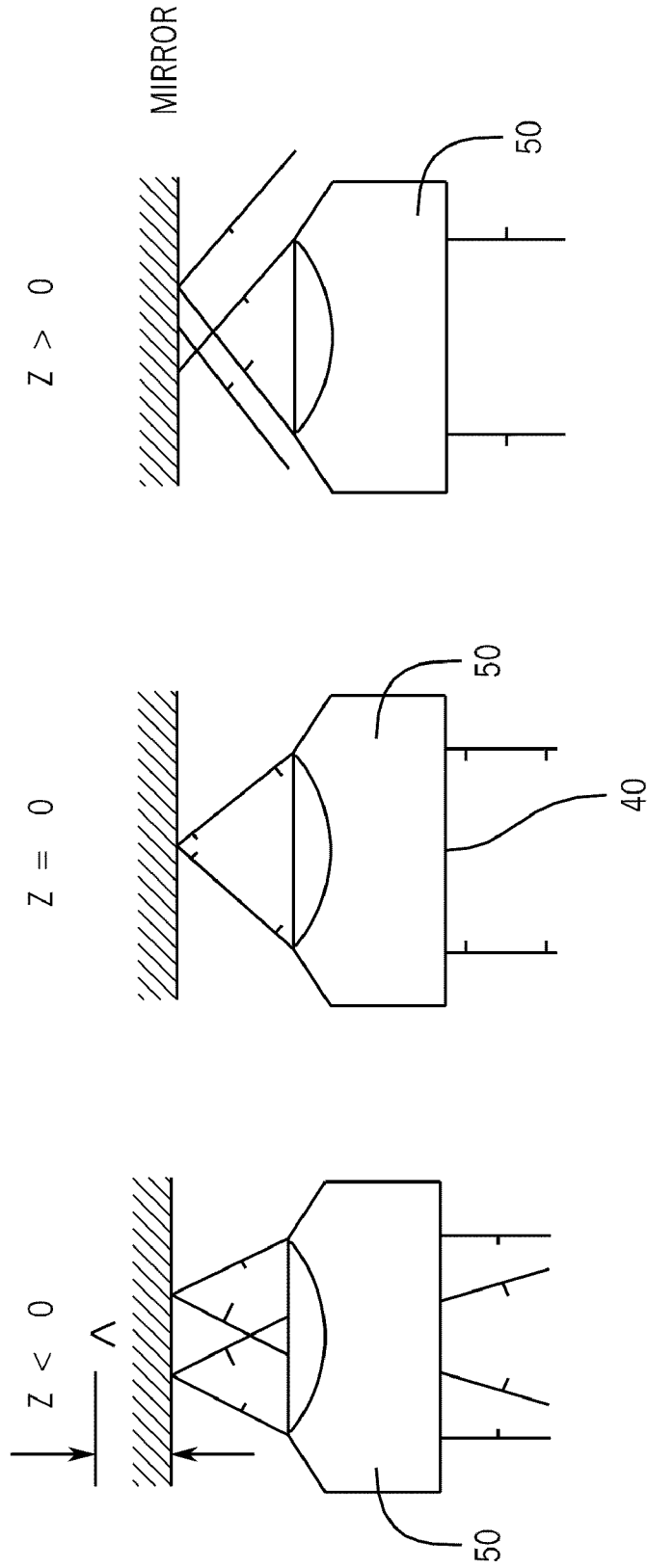


FIG. 2C

FIG. 2B

FIG. 2A

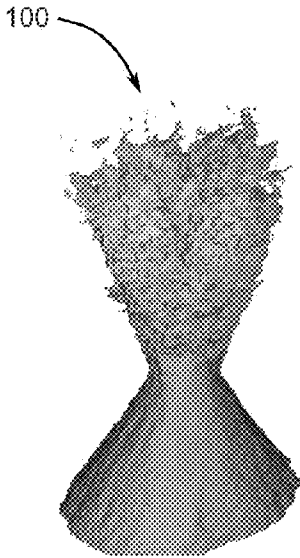


FIG. 3A

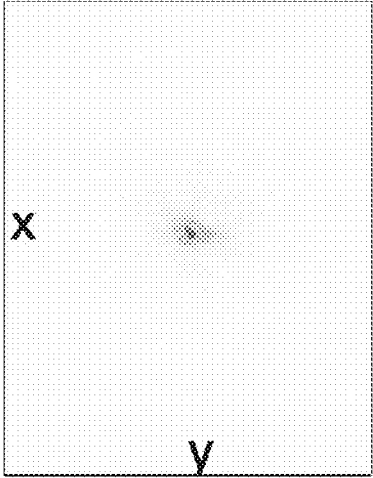


FIG. 3B

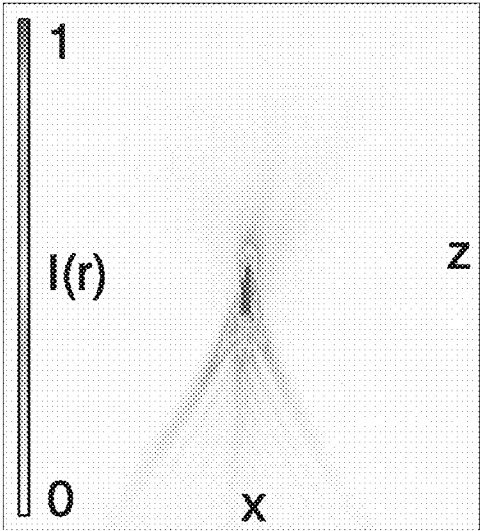


FIG. 3C

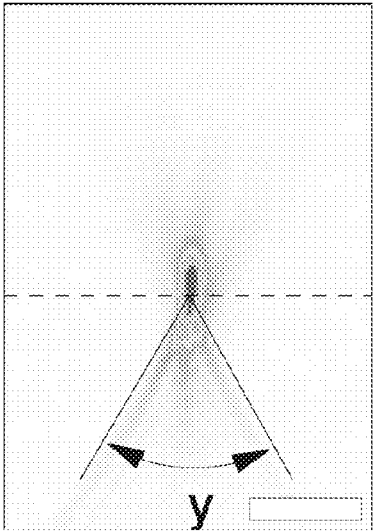


FIG. 3D

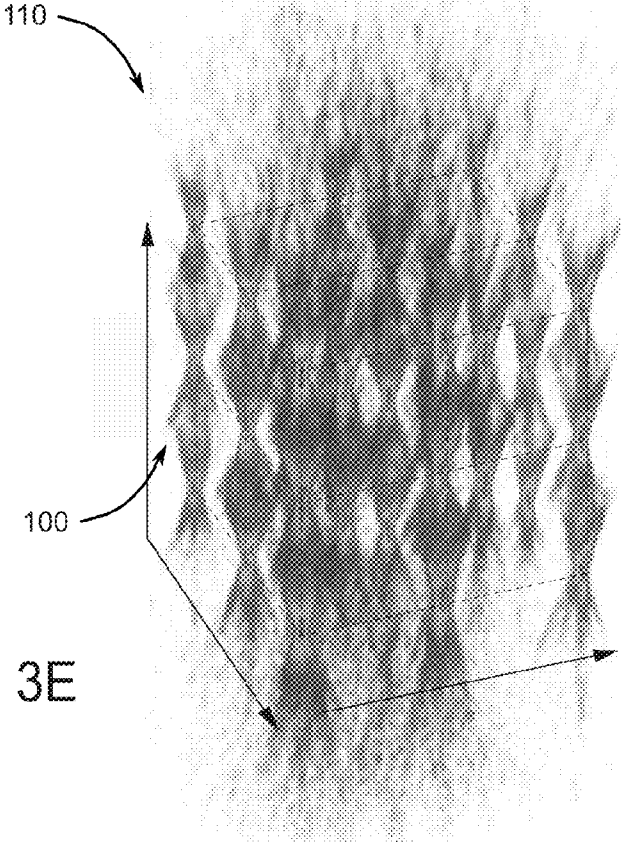


FIG. 3E

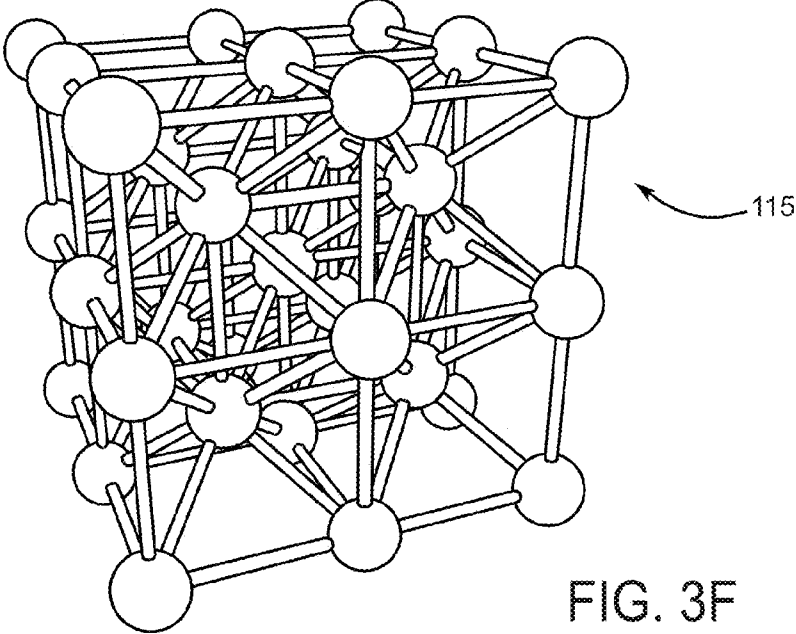


FIG. 3F

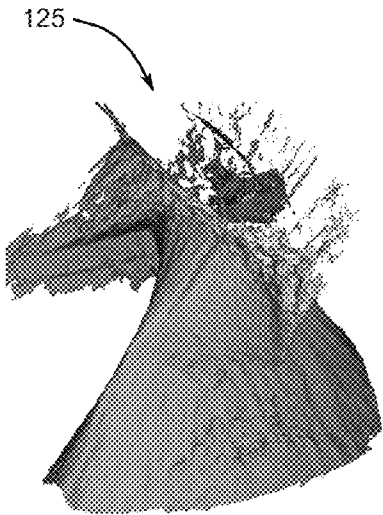


FIG. 4A

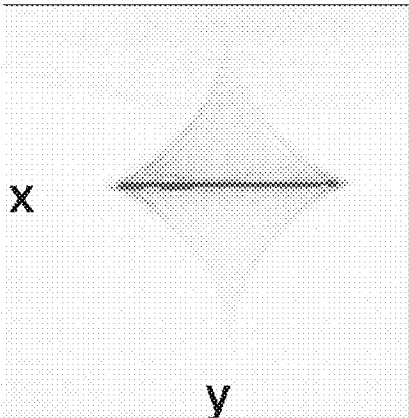


FIG. 4B

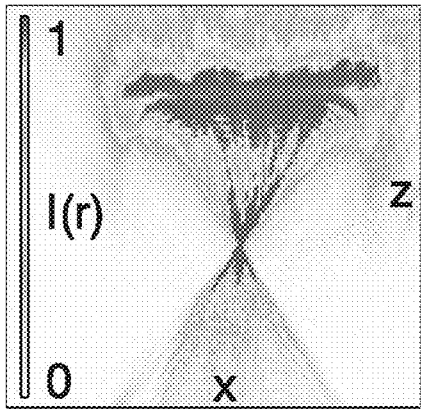


FIG. 4D

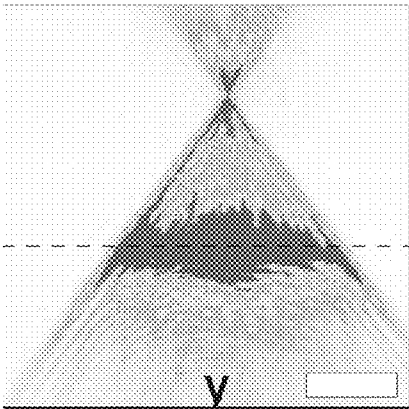


FIG. 4C

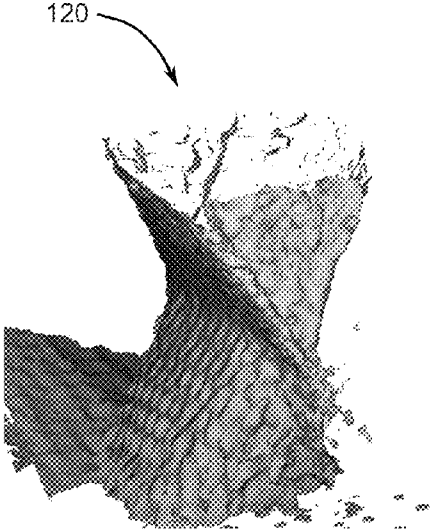


FIG. 5A

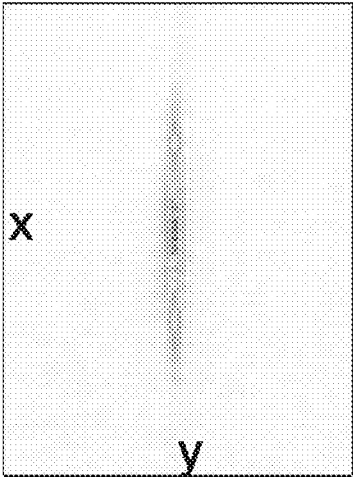


FIG. 5B

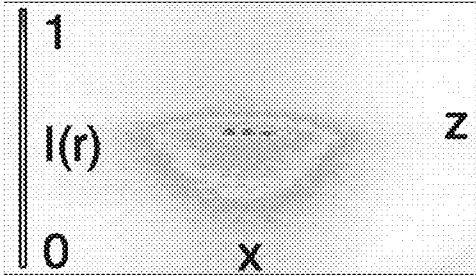


FIG. 5D

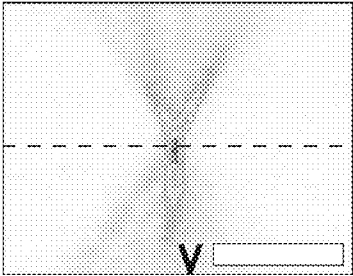


FIG. 5C



# VOLUMETRIC IMAGING OF HOLOGRAPHIC OPTICAL TRAPS

## CROSS-REFERENCE TO RELATED PATENT APPLICATIONS

This application is a continuation of U.S. application Ser. No. 11/974,716, filed Oct. 16, 2007, which claims priority from U.S. Provisional Application 60/852,252, filed Oct. 17, 2006, both of which are incorporated herein by reference in their entirety.

This invention is directed toward volumetric imaging of holographic optical traps. More particularly, the invention is directed to a method and system for creating arbitrary pre-selected three-dimensional (3D) configurations of optical traps having individually specified optical characteristics. Holographic techniques are used to modify individual trap wavefronts to establish pre-selected 3D structures having predetermined properties and are positionable independently in three dimensional space to carry out a variety of commercially useful tasks.

The United States Government has certain rights in this invention pursuant to a grant from the National Science Foundation through grant number DMR-0451589.

## BACKGROUND OF THE INVENTION

There is, a well developed technology of using single light beams to form an optical trap which applies optical forces from the focused beam flight to confine an object to a particular location in space. These optical traps, or optical tweezers, have enabled fine scale manipulation of objects for a variety of commercial purposes. In addition, line traps, or extended optical tweezers, have been created which act as a one dimensional potential energy landscape for manipulating mesoscopic objects. Such line traps can be used to rapidly screen interactions between colloidal and biological particles which find uses in biological research, medical diagnostics and drug discovery. However, these applications require methods of manipulation diagnostics and drug discovery. However, these applications require methods of manipulation for projecting line traps with precisely defined characteristics which prevent their use in situations with high performance demands. Further, the low degrees of freedom and facility of use for such line traps reduces the ease of use and limits the types of uses available.

## SUMMARY OF THE INVENTION

The facility and range of applications of optical traps is greatly expanded by the method and system of the invention in which 3D intensity distributions are created by holography. These 3D representations are created by holographically translating optical traps through an optical train's focal plane and acquiring a stack of two dimensional images in the process. Shape phase holography is used to create a pre-selected 3D intensity distribution which has substantial degrees of freedom to manipulate any variety of object or mass for any task.

Various aspects of the invention are described hereinafter; and these and other improvements are described in greater detail below, including the drawings described in the following section.

## BRIEF DESCRIPTION OF THE DRAWINGS

FIG. 1 illustrates an optical train for performing a method of the invention;

FIG. 2A illustrates a particular optical condition with  $z < 0$  for an objective lens in the system of FIG. 1; FIG. 2B illustrates the optical condition for  $z = 0$  for the objective lens of FIG. 1 and FIG. 2C illustrates the optical condition for  $z > 0$  for the objective lens of FIG. 1;

FIG. 3A illustrates a 3D reconstruction of an optical tweezer propagating along the  $z$  axis; FIG. 3B illustrates a cross-section of FIG. 3A along an  $xy$  plane; FIG. 3C illustrates a cross-section of FIG. 3A along a  $yz$  plane; FIG. 3D illustrates a cross-section of FIG. 3A along an  $xz$  plane; FIG. 3E illustrates a volumetric reconstruction of 35 optical tweezers arranged in a body-centered cubic lattice of the type shown in FIG. 3F;

FIG. 4A illustrates a 3D reconstruction of a cylindrical lens line optical tweezer; FIG. 4B illustrates a cross-section of FIG. 4A along an  $xy$  plane; FIG. 4C illustrates a cross-section of FIG. 4A along a  $yz$  plane; and FIG. 4D illustrates a cross-section of FIG. 4A along an  $xz$  plane; and

FIG. 5A illustrates a 3D reconstruction of a holographic optical trap featuring diffraction-limited convergence to a single focal plane; FIG. 5B illustrates a cross-section of FIG. 5A along a  $xy$  plane; FIG. 5C illustrates a cross-section of FIG. 5A along a  $yz$  plane; and FIG. 5D illustrates a cross-section of FIG. 5A along an  $xz$  plane.

## DETAILED DESCRIPTION OF PREFERRED EMBODIMENTS

An optical system for performing, methods of the invention is illustrated generally at 10 in FIG. 1. A beam of light 20 is output from a frequency-doubled solid-state laser 30, preferably a Coherent Verdi system operating at a wavelength of  $\lambda = 532$  nm. The beam of light 20 is directed to an input pupil 40 of a high-numerical-aperture objective lens 50, preferably a Nikon 100xPlan Apo, NA 1.4, oil immersion system that focuses the beam of light 20 into an optical trap (not shown). The beam of light 20 is imprinted with a phase-only hologram by a computer-addressed liquid-crystal spatial light modulator 60 ("SLM 60"), preferably a Hamamatsu X8267 PPM disposed in a plane conjugate to the objective lens' 50 input plane. Computer 95 executes conventional computer software to generate the appropriate hologram using the SLM 60. As a result, the light field,  $\psi(r)$ , in the objective lens' 50 focal plane is related to the field  $\psi(\rho)$  in the plane of the SLM 60 by the Fraunhofer transform,

$$\psi(r) = -\frac{i}{\lambda f} \int_{\Omega} \psi(\rho) \exp\left(-i\frac{2\pi}{\lambda f} r \cdot \rho\right) d^2 \rho, \quad (1)$$

where  $f$  is the objective's focal length, where  $\Omega$  is the optical train's aperture, and where we have dropped irrelevant phase factors. Assuming that the beam of light 20 illuminates the SLM 60 with a radially symmetric amplitude profile,  $u(\rho)$ , and uniform phase, the field in the SLM's plane may be written as,

$$\psi(\rho) = u(\rho) \exp(i\phi(\rho)), \quad (2)$$

where  $\phi(\rho)$  is the real-valued phase profile imprinted on the beam of light 20 by the SLM 60. The SLM 60 in our preferred form of the system 10 imposes phase shifts between 0 and  $2\pi$  radians at each pixel of a  $768 \times 768$  array. This two-dimen-

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sional phase array can be used to project a computer-generated phase-only hologram,  $\phi(\rho)$ , designed to transform the single optical tweezer into any desired three-dimensional configuration of optical traps, each with individually specified intensities and wavefront properties.

Ordinarily, the pattern of holographic optical traps would be put to use by projecting it into a fluid-borne sample mounted in the objective lens' **50** focal plane. To characterize the light field, we instead mount a front-surface mirror **70** in the sample plane. This mirror **70** reflects the trapping light back into the objective lens **50**, which transmits images of the traps through the partially reflecting mirror **70** to a charge-coupled device (CCD) camera **80**, preferably a NEC TI-324AII. In our implementation, the objective lens **50**, the camera **80** and camera eyepiece (not shown), are mounted in a conventional optical Microscope (not shown) and which is preferably a Nikon TE-2000U.

Three-dimensional reconstructions of the optical traps' intensity distribution can be obtained by translating the mirror **70** relative to the objective lens **50**. Equivalently, the traps can be translated relative to the mirror **70** by superimposing the parabolic phase function,

$$\varphi_z(\rho) = -\frac{\pi\rho^2z}{\lambda f^2}, \quad (3)$$

onto the hologram  $\phi_0(\rho)$  encoding a particular pattern of traps. The combined hologram,  $\phi_0(\rho) = \phi_0(\rho) + \phi_z(\rho) \bmod 2\pi$ , projects the same pattern of traps as  $\phi_0(\rho)$  but with each trap translated by  $-z$  along optical axis **90** of the system **10**. The resulting image obtained from the reflected light represents a cross-section of the original trapping intensity at distance  $z$  from the focal plane of the objective lens **50**. Translating the traps under software control by computer **95** is particularly convenient because it minimizes changes in the optical train's properties due to mechanical motion and facilitates more accurate displacements along the optical axis **90**. Images obtained at each value of  $z$  are stacked up to yield a complete volumetric representation of the intensity distribution.

As shown schematically in FIGS. **2A-2C**, the objective lens **50** captures essentially all of the reflected light for  $z < 0$ . For  $z > 0$ , however, the outermost rays of the converging trap are cut off by the objective lens' **50** output pupil **105**, and the contrast is reduced accordingly. This could be corrected by multiplying the measured intensity field by a factor proportional to  $z$  for  $z > 0$ . The appropriate factor, however, is difficult to determine accurately, so we present only unaltered results.

FIG. **3A** shows a conventional optical tweezer **100** reconstructed in the manner described hereinbefore and displayed as an iso-intensity surface at 5 percent peak intensity and in three cross-sections (FIGS. **3B-3D**). The representation in FIG. **3A** is useful for showing the overall structure of the converging light, and the cross-sections of FIGS. **3B-3D** provide an impression of the three dimensional light field that will confine an optically trapped object. The angle of convergence of  $63^\circ$  in immersion oil obtained from these data is consistent with an overall numerical aperture of 1.4. The radius of sharpest focus,  $r_{min} \approx 0.2 \mu\text{m}$ , is consistent with diffraction-limited focusing of the beam of light **20**.

These results highlight two additional aspects of this reconstruction technique. The objective lens **50** is designed to correct for spherical aberration when the beam of light **20** passing through water is refracted by a glass coverslip. Without this additional refraction, the projected optical trap **100** actually is degraded by roughly  $20\lambda$  of spherical aberration,

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introduced by the objective lens **50**. This reduces the apparent numerical aperture and also extends the trap's focus along the  $z$  axis. The trap's effective numerical aperture in water would be roughly 1.2. The effect of spherical aberration can be approximately corrected by pre-distorting the beam of light **20** with the additional phase profile,

$$\varphi_a(\rho) = \frac{\alpha}{\sqrt{2}}(6x^4 - 6x^2 + 1), \quad (4)$$

the Zernike polynomial describing spherical aberration. The radius,  $x$ , is measured as a fraction of the optical train aperture, and the coefficient  $\alpha$  is measured in wavelengths of light. This procedure is used to correct for small amount of aberration present in practical optical trapping systems to optimize their performance.

This correction was applied to an array **110** of 35 optical tweezers shown as a three-dimensional reconstruction in FIG. **3E**. These optical traps **100** are arranged in a three-dimensional body-centered cubic (BCC) lattice **115** shown in FIG. **3F** with a  $10.8 \mu\text{m}$  lattice constant. Without correcting for spherical aberration, these traps **100** would blend into each other along the optical axis **90**. With correction, their axial intensity gradients are clearly resolved. This accounts for holographic traps' ability to organize objects along the optical axis.

Correcting for aberrations reduces the range of displacements,  $z$ , that can be imaged. Combining  $\varphi_a(\rho)$  with  $\varphi_z(\rho)$  and  $\phi_0(\rho)$  increases gradients in  $\phi(\rho)$ , particularly for larger values of  $\rho$  near the edges of the diffraction optical element. Diffraction efficiency falls off rapidly when  $|\nabla\phi(\rho)|$  exceeds  $2\pi/\Delta\rho$ , the maximum phase gradient that can be encoded on the SLM **60** with pixel size  $\Delta\rho$ . This problem is exacerbated when  $\phi_0(\rho)$  itself has large gradients. In a preferred embodiment more complex trapping patterns without aberration are prepared. In particular, we use uncorrected volumetric imaging to illustrate the comparative advantages of the extended optical traps **100**.

The extended optical traps **100** have been projected in a time-shared sense by rapidly scanning a conventional optical tweezer along the trap's intended contour. A scanned trap has optical characteristics as good as a point-like optical tweezer, and an effective potential energy well that can be tailored by adjusting the instantaneous scanning rate. Kinematic effects due to the trap's motion can be minimized by scanning rapidly enough. For some applications, however, continuous illumination or the simplicity of an optical train with no scanning capabilities can be desirable.

Continuously illuminated line traps have been created by expanding an optical tweezer **125** along one direction (see FIG. **4A**). This can be achieved, for example, by introducing a cylindrical lens component such as by element **130** (see FIG. **1**) into the objective's input plane. Equivalently, a cylindrical-lens line tweezer can be implemented by encoding the function  $\phi_c(\rho) = \pi z_0 \rho_x^2 / (\lambda f^2)$  on the SLM **60**. The result, shown in FIGS. **4A-4D** appears best useful in the plane of best focus,  $z = z_0$ , with the point-like tweezer having been extended to a line with nearly parabolic intensity and a nearly Gaussian phase profile. The three-dimensional reconstruction, however, reveals that the cylindrical lens component merely introduces a large amount of astigmatism into the beam of light **20**, creating a second focal line perpendicular to the first. This is problematic for some applications because the astigmatic beam's axial intensity gradients are far weaker than a conventional optical tweezer's. Consequently, cylindrical-lens

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line traps typically cannot localize objects against radiation pressure along the optical axis **90**.

Replacing the single cylindrical lens with a cylindrical Keplerian telescope for the element **130** eliminates the astigmatism and thus creates a stable three-dimensional optical trap. Similarly, using the objective lens **50** to focus two interfering beams creates an interferometric optical trap capable of three-dimensional trapping. These approaches, however, offer little control over the extended traps intensity profiles, and neither affords control over the phase profile.

Shape-phase holography provides absolute control over both the amplitude and phase profiles of an extended form of the optical trap **100** at the expense of diffraction efficiency. It also yields traps with optimized axial intensity gradients, suitable for three-dimensional trapping. If the line trap is characterized by an amplitude profile  $\hat{u}(\rho_x)$  and a phase profile  $\hat{p}(\rho_x)$  along the  $\hat{\rho}_x$  direction in the objective's focal plane, then the field in the SLM plane is given from Eq. (1) as,

$$\psi(\rho)=u(\rho_x)\exp(ip(\rho_x)), \quad (5)$$

where the phase  $p(\rho_x)$  is adjusted so that  $u(\rho_x) \geq 0$ . Shape-phase holography implements this one-dimensional complex wavefront profile as a two-dimensional phase-only hologram,

$$\varphi(\rho) = \begin{cases} p(\rho_x), & S(\rho) = 1 \\ q(\rho), & S(\rho) = 0, \end{cases} \quad (6)$$

where the shape function  $S(\rho)$  allocates a number of pixels along the row  $\rho_y$ , proportional to  $u(\rho_x)$ . One particularly effective choice is for  $S(\rho)$  to select pixels randomly along each row in the appropriate relative numbers. The unassigned pixels then are given values  $q(\rho)$  that redirect the excess light away from the intended line. Typical results are presented in FIG. 5A.

Unlike the cylindrical-lens trap, the holographic line trap **130** in FIGS. 5A-5D focuses as a conical wedge to a single diffraction-limited line in the objective's focal plane. Consequently, its transverse angle of convergence is comparable to that of an optimized point trap. This means that the holographic line trap **120** has comparably strong axial intensity gradients, which explains its ability to trap objects stably against radiation pressure in the z direction.

The line trap's transverse convergence does not depend strongly on the choice of intensity profile along the line. Its three-dimensional intensity distribution, however, is very sensitive to the phase profile along the line. Abrupt phase changes cause intensity fluctuations through Gibbs phenomenon. Smoother variations do not affect the intensity profile along the line, but can substantially restructure the beam. The line trap **120** created by the cylindrical lens element **130** for example, has a parabolic phase profile. Inserting this choice into Eq. (2) and calculating the associated shape-phase hologram with Eqs. (1) and (6) yields the same cylindrical lens phase profile. This observation opens the door to applications in which the phase profile along a line can be tuned to create a desired three-dimensional intensity distribution, or in which the measured three-dimensional intensity distribution can be used to assess the phase profile along the line. These applications will be discussed elsewhere.

The foregoing description of embodiments of the present invention have been presented for purposes of illustration and description. It is not intended to be exhaustive or to limit the present invention to the precise form disclosed, and modifications and variations are possible in light of the above teachings or may be acquired from practice of the present inven-

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tion. The embodiments were chosen and described in order to explain the principles of the present invention and its practical application to enable one skilled in the art to utilize the present invention in various embodiments, and with various modifications, as are suited to the particular use contemplated.

What is claimed is:

**1.** A system for obtaining a three-dimensional cross-section of the trapping intensity of trapping light for at least one of characterizing the trapping light and for performing tasks on a sample, comprising:

- an optical train;
- a source for providing a beam of light to the optical train;
- a computer for applying a predetermined hologram to the beam of light to generate trapping light;
- a mirror for reflecting the trapping light;
- a sensor for obtaining a plurality of three-dimensional cross-sections of trapping intensity of the trapping light from the reflected light thereby enabling at least one of analysis of the trapping intensity and use of the trapping intensity cross-section for guiding use of the trapping light on the sample.

**2.** The system as defined in claim **1** further including a front surface form of the mirror with the trapping light reflected off the front surface mirror into an objective lens and further transmits images of the trapping light through a partially reflecting mirror into a camera.

**3.** The system as defined in claim **1** wherein the trapping light is translated relative to the mirror by the computer superimposing a phase function on the trapping light.

**4.** The system as defined in claim **1** wherein an image is constructed from the reflected light which represents a cross-section of the trapping intensity reconstructed at least one of (1) a plurality of distances z from a focal plane of the optical train; and (2) with a plurality of the images being used to create a volumetric representation of the trapping intensity.

**5.** The system as defined in claim **1** wherein the computer determines a hologram to carry out at least one of the analysis of the trapping light or use of the cross-section for operating on the sample and further includes having the optical train with a mirror disposed in the sample plane and operating on the beam of light to process a light field of the trapping light.

**6.** The system as defined in claim **5** wherein the hologram includes a parabolic phase function to enable translating the trapping light, the system configured to create a plurality of cross-sections of trapping intensity by at least one of (1) the mirror disposed in the sample plane translating relative to an objective lens of the optical trapping and (2) the trapping light translating relative to a fixed form of the mirror.

**7.** The system as defined in claim **6** wherein the parabolic phase function comprises,

$$\varphi_z(\rho) = -\frac{\pi\rho^2 z}{\lambda f^2},$$

where,

- $\phi$ =hologram phase value at position  $\rho$ ;
- z=distance along an optical axis of the optical train;
- $\lambda$ =wavelength of the light;
- f=objective lens focal length;
- $\rho$ =position in the hologram.

**8.** The system as defined in claim **6** wherein a computer program executed by the computer determines the hologram for translating the trapping light.

9. The system as defined in claim 5 wherein the phase only hologram comprises,

$$\varphi(\rho) = \begin{cases} p(\rho_x), & S(\rho) = 1 \\ q(\rho), & S(\rho) = 0, \end{cases}$$

where S (ρ) is a shape function which allocates a number of pixels along row, ρ;

p (ρ) is a phase profile and q (ρ) are values along the row, ρ, for unassigned pixels along the row and which redirect excess light from an intended line.

10. The system as defined in claim 5 wherein the sensor provides analysis data defining a two dimensional cross section of original trapping density of the predetermined trapping light configuration.

11. The system as defined in claim 10 wherein the data includes a plurality of the two dimensional cross sections.

12. The system as defined in claim 1 wherein the trapping light is configured to manipulate an object in the same plane.

13. The system as defined in claim 12 further including the step of passing the beam of light through an objective lens of the optical train and applying a phase profile to the trapping light, thereby enabling a plurality of trapping lights to organize selected ones of the objects along an optical axis of the optical train.

14. The system as defined in claim 13 wherein the phase profile comprises,

$$\varphi_o(\rho) = \frac{a}{\sqrt{2}}(6x^4 - 6x^2 + 1),$$

thereby correcting for spherical aberration where x is distance measured as a fraction of the optical train aperture and “a” is a coefficient measured in wavelengths of light.

15. The system as defined in claim 12 further including the step of forming a single trapping light and rapidly scanning the single trapping light along a predetermined configuration to enable manipulation of the sample.

16. The system as defined in claim 1 further including an objective lens disposed in the optical train and further includes a cylindrical lens component disposed in an input plane of the objective lens.

17. The system as defined in claim 1 wherein the predetermined hologram includes a cylindrical-lens line component.

18. The system as defined in claim 17 wherein the predetermined hologram includes the function  $\phi_c(\rho) = \pi Z_0 \rho_x^2 / (\lambda f^2)$ .

19. The system as defined in claim 1 further including in the optical train a Keplerian telescope for eliminating astigmatism, thereby creating a stable form of three dimensional trapping light.

20. The system as defined in claim 19 wherein the optical train includes an SLM having an associated plane and the field in the associated plane is given by,  $\psi(\rho) = u(\rho_x) \exp(ip(\rho_x))$ .

21. The system as defined in claim 1 wherein the trapping light comprises a hologram constructed of,

- a. an amplitude profile  $\tilde{u}(\rho_x)$ ,
- b. a phase profile  $\hat{p}(\rho_x)$  with an objective focal plane direction  $\hat{\rho}_x$ .

\* \* \* \* \*